

## KU5DSCMAT302

### BASIC ABSTRACT ALGEBRA

Semester	Course Type	Course Level	Course Code	Credits	Total Hours
V	DSC	300-399	KU5DSCMAT302	4	60

Learning Approach (Hours/ Week)			Marks Distribution			Duration of ESE (Hours)
Lecture	Practical/ Internship	Tutorial	CE	ESE	Total	
4		1	30	70	100	2

#### Course Description

This course introduces the abstract structures like group, rings, integral domains and fields and to discuss basic properties and problems in groups.

#### Course Prerequisite

Set and Functions.

#### Course Outcomes

CO No.	Expected Outcome	Learning Domains
1	Comprehend binary operations and groups.	Understand
2	Classify abelian groups and non-abelian groups.	Understand
3	Understand permutation groups.	Understand
4	Determining the subgroups of groups, cyclic subgroups and cyclic groups.	Apply
5	Comprehend generating sets, group of permutations and cosets	Understand
6	Understand Factor groups, Rings, Fields and integral domain	Understand

Mapping of Course Outcomes to PSOs							
	PSO 1	PSO 2	PSO 3	PSO 4	PSO 5	PSO 6	PSO 7
CO 1	✓						
CO 2	✓						
CO 3	✓		✓				

CO 4	✓						
CO 5	✓	✓					
CO 6	✓						

## COURSE CONTENTS

### Contents for Classroom Transaction

M O D U L E	U N I T	DESCRIPTION	HOURS
<b>I</b>	<b>Groups</b>		<b>14</b>
	1	<b>Binary operations</b>	
		a) Definitions and Examples	
		b) Tables	
	2	<b>Groups</b>	
		a) Definition and Examples	
		b) Elementary Properties of Groups	
		c) Group Isomorphisms	
		d) Properties of Group Tables	
3	<b>Abelian Examples</b>		
<b>II</b>	<b>Subgroups and Cyclic groups</b>		<b>14</b>
	1	<b>Nonabelian Examples</b>	
		a) Notation and Terminology	
		b) Permutations	
		c) Disjoint Cycles	
		d) The Dihedral Group	
	2	<b>Subgroups</b>	
		a) Subsets and Subgroups	
	b) Cyclic Subgroups		

	3	<b>Cyclic Groups</b>	
		a) Elementary Properties of Cyclic Groups	
		b) The structure of Cyclic Groups	
		c) Subgroups of Finite Cyclic Groups	
<b>III</b>	<b>Generating Sets and Structure of Groups</b>		<b>13</b>
	1	<b>Generating Sets</b>	
	2	<b>Groups of Permutations</b>	
		a) Group homomorphism	
		b) Cayley's Theorem	
		c) Even and Odd Permutations	
	3	<b>Cosets and the Theorem of Lagrange</b>	
		a) Cosets	
		b) The Theorem of Lagrange	
		c) Cosets Left and Right	
<b>IV</b>	<b>Factor Groups, Rings and Fields</b>		<b>14</b>
	1	<b>Factor Groups</b>	
	2	<b>Rings and Fields</b>	
		a) Definitions and Basic Properties	
		b) Homomorphisms and Isomorphisms	
	3	c) Multiplicative Questions: Fields	
		<b>Integral Domains</b>	
		a) Divisors of Zero and Cancellation	
		b) Integral Domains	
<b>V</b>	<b>Teacher Specific Module</b>		<b>5</b>
	<i>Directions</i>		
	Omitted Proofs of the above sections.		
	Cayley Digraphs		
	Plane Isometries		

### Essential Readings

1. John B. Fraleigh, A First Course in Abstract Algebra, Eighth Edition, Pearson.

### Reference Distribution

Module	Unit	Reference No.	Sections	Remarks
<b>I</b>	1	1	1.1 to 1.30	
	2		2.1 to 2.23	
	3		3.1 to 3.5	
<b>II</b>	1		4.1 to 4.21	Omitting the proofs of 4.17 and 4.21
	2		5.1 to 5.26	
	3		6.1 to 6.21	Omitting the proofs of 6.2, 6.10 and 6.15
<b>III</b>	1		7.1 to 7.6	
	2		8.1 to 8.25	Omitting the proofs of 8.5 and 8.19
	3		10.1 to 10.20	Omitting the proof of 10.17
<b>IV</b>	1		12.1 to 12.11	
	2		22.1 to 22.18	
	3		23.1 to 23.14	

### Suggested Readings

1. J.A Gallian, Contemporary Abstract Algebra, Narosa.
2. I.N Herstein, Topics in Algebra (2<sup>nd</sup> edition), Wiley
3. M. Artin, Algebra, Prentice Hall

### Assessment Rubrics

Evaluation Type		Marks
End Semester Evaluation		<b>70</b>
Continuous Evaluation		<b>30</b>
a)	Test Paper*	12
b)	Assignment	12
c)	Seminar/ Viva-voce	6
<b>Total</b>		<b>100</b>

\* A student has to appear for at least two written tests. Average mark of best two tests is to be considered for internal mark.